

Covert the following to a...

Log

Exponential

1. $3^x = 32$

$$\log_3 32 = x$$

2. $r^{ab} = 17$

$$\log_r 17 = ab$$

3. $(7)^{x-2} = 8$

$$\log_7 8 = x-2$$

4. $\log(x-3) = 2$

$$10^2 = x-3$$

5. $\ln x = 5$

$$e^5 = x$$

6. $\log_4(2x-1) = 2$

$$4^2 = 2x-1$$

Properties of Logs

| | |
|--------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------|
| <p><u>Product Property</u></p> $\log_b mn = \log_b m + \log_b n$ | <p><u>Quotient Property</u></p> $\log_b \left(\frac{m}{n}\right) = \log_b m - \log_b n$ |
| <p><u>Power Property</u></p> $\log_b m^n = n \log_b m$ <p>exponent becomes a coefficient</p> | <p>*<u>Change of Base Property</u></p> $\log_b m = \frac{\log_r m}{\log_r b} = \frac{\log \text{ of } m}{\log \text{ base } b}$ |
| <p><u>One-to-One Property</u></p> <p>If $\log_b m = \log_b n$ then $m = n$.</p> | <p><u>Inverse Property</u></p> $\log_b b^m = m \text{ and } b^{\log_b m} = m$ |

$$\begin{aligned} &\log_b b^m \\ &m \log_b b \\ &m(1) \\ &m \end{aligned}$$

Example 1 Using the Product, Quotient, & Power Properties

$$\log_b mn = \log_b m + \log_b n$$

$$\log_b \left(\frac{m}{n}\right) = \log_b m - \log_b n$$

$$\log_b m^n = n \log_b m$$

Given: $\begin{cases} \log_{13} 12 \approx 0.969 \\ \log_{13} 10 \approx 0.898 \end{cases}$

A] Find $\log_{13} 100 =$

$$\begin{aligned} & \log_{13} 10^2 \\ & 2 \log_{13} 10 \\ & 2(.898) = 1.796 \end{aligned}$$

B] Find $\log_{13} 120 =$

$$\begin{aligned} & \log_{13} 12 \cdot 10 \\ & \log_{13} 12 + \log_{13} 10 \\ & .969 + .898 = 1.867 \end{aligned}$$

$$\frac{5}{6} = \frac{10}{12}$$

C] Find $\log_{13} \left(\frac{5}{6}\right) = \log_{13} \left(\frac{10}{12}\right)$

$$\log_{13} 5 - \log_{13} 6$$

$$\log_{13} (10) - \log_{13} (12)$$

$$.898 - .969 = -.071$$

D] Find $\log_{13} \left(\frac{72}{5}\right) = \log_{13} \left(\frac{144}{10}\right)$

$$\log_{13} 72 + \log_{13} 5 \quad \log_{13} 144 - \log_{13} 10$$

$$\log_{13} 12 \cdot 6 + \log_{13} 5 \quad \log_{13} 12 \cdot 12 - \log_{13} 10$$

$$\log_{13} 12 + \log_{13} 6 + \log_{13} 5 \quad \log_{13} 12 + \log_{13} 12 - \log_{13} 10$$

$$.969 + .969 + .898 \quad .969 + .969 - .898$$

$$.969 + \log_{13} 6 + \log_{13} 5$$

$$1.04$$

Example 2 Using the Inverse Properties

$$\log_b b^m = m \quad \text{and} \quad b^{\log_b m} = m$$

Use the powers table to make the base of the log and object of the log match. Then use the property

A) $\log_9 3^{2x}$

$$\log_9 (3^2)^x \rightarrow \log_9 (9)^x \rightarrow \textcircled{X}$$

D) $4^{\log_4 x^3}$

$$\textcircled{X^3}$$

B) $\log_2 16^x$

$$\log_2 (2^4)^x \rightarrow \log_2 2^{4x} \rightarrow \textcircled{4x}$$

E) $3^{2\log_3 x}$

$$3^{\log_3 x^2} \quad \textcircled{X^2}$$

C) $\log_{27} 3^{6x}$

$$\log_{27} (3^3)^{2x} \rightarrow \log_{27} (27)^{2x} \rightarrow \textcircled{2x}$$

F) $125^{\log_5 2x}$

$$(5^3)^{\log_5 2x}$$

$$5^{\log_5 (2x)^3}$$

$$(2x)^3 \text{ or } 8x^3$$

⑥

$$2\log_8 x - 10\log_8 y$$

$$\log_8 x^2 - \log_8 y^{10}$$

$$\log_8 \frac{x^2}{y^{10}}$$

⑪ $\log_7 (u^4 \cdot v)^3$

$$\log_7 u^{12} \cdot v^3$$

$$\log_7 u^{12} + \log_7 v^3$$

$$12\log_7 u + 3\log_7 v$$

